

Understanding the Factors that Influence the Probability and Time to Streetcar Bunching Incidents

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1 **UNDERSTANDING THE FACTORS THAT INFLUENCE THE PROBABILITY AND**
2 **TIME TO STREETCAR BUNCHING INCIDENTS**

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1 **ABSTRACT**

2 Bunching is a well known operational problem for transit agencies and it has negative impacts on
3 service quality and users' perception. While there has been a substantial amount of literature on
4 understanding the causes of bus bunching and strategies used to mitigate the effects of this
5 problem, there has been little research on streetcar bunching. Although bus and streetcar systems
6 share many similarities, one major difference between the two is that streetcars cannot overtake
7 each other. This makes bunching in streetcar networks more critical to the reliability of the
8 system and an important topic that requires more in-depth understanding. This research aims at
9 understanding the factors that impact the likelihood of streetcar bunching and to investigate in
10 more detail the external and internal factors that impact the time to bunching since the departure
11 of a streetcar from its route's terminal. To achieve the first goal, the study uses a binary logistic
12 regression model, while it uses survival analysis - accelerated failure time (AFT) model to
13 address the second goal. The study utilizes automatic vehicle location (AVL) system data
14 acquired from the Toronto Transit Commission (TTC), the transit provider for the City of
15 Toronto. The models' results show that headway deviations at terminals both increase the
16 probability of bunching and accelerate the time to bunching. The discrepancy in vehicle types
17 between two successive streetcars also increases the likelihood of bunching and accelerates the
18 time to bunching. This study offers a better understanding of the factors that impact streetcar
19 service bunching, which is an important component of transit service reliability.

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23 **Keywords:** Streetcar, bunching, reliability, accelerated failure time (AFT) model, survival
24 analysis

1 INTRODUCTION

2 Public transit systems face many different operational problems and disruptions that can degrade
3 the quality and reliability of service. One of the most common disruptions is vehicle bunching.
4 Bunching occurs when two or more consecutive vehicles on the same route are unable to
5 maintain their scheduled headways and end up following each other too closely. Bunching
6 causes serious challenges to both the passengers and operators. For the passengers, bunching
7 causes longer or variable wait times and vehicle overcrowding, which both contribute to
8 reducing users' satisfaction. For the transit agencies, bunching leads to increased costs due to
9 the inefficient use of resources since overcrowded vehicles at the front of a bunch would be
10 followed closely by near-empty ones. Bunching also impacts the overall image of transit
11 agencies, making it harder to attract new transit riders and retain the existing ones (1, 2). For all
12 these reasons, bunching has been a popular topic in the literature over the past two decades.

13 Bunching is a well known problem that is frequently experienced in the City of Toronto,
14 not only along bus routes but even worse along streetcar routes (3). Although buses and
15 streetcars share many similarities, one major difference between the two is that streetcars cannot
16 overtake each other since they are limited to the path of their track infrastructure. This subtle
17 difference makes bunching incidents more critical to the streetcar system quality than buses,
18 which can overtake each other. The problem is exasperated in Toronto by the very high
19 frequency of streetcar services relative to bus services. Yet, there is very little literature found on
20 streetcar bunching. This is likely due to the fact that streetcars are an uncommon transit vehicle
21 mode and are utilized in very few cities around the world. However, many cities are now
22 planning or in the construction stage of building new light rail or streetcar systems including
23 Minneapolis, Kansas City, and Montreal (4). For example, in 2016, Kansas City introduced a
24 new streetcar line, with further plans of expansion (5). Streetcar technology may be mature, but
25 streetcar bunching is a topic that needs a more comprehensive study as streetcar and light rail
26 systems become more popular.

27 The TTC streetcar system is one of the largest in North America. In 2016, the TTC
28 operated 11 streetcar routes, covering 338 km (6). Approximately 300,000 passengers ride the
29 streetcars on a typical weekday. Headways range from 2 to 10 minutes on the streetcar network
30 with the average being approximately 4 minutes on weekdays during the morning and afternoon
31 peak periods. The TTC has a fleet of 250 streetcar vehicles using a combination of three
32 different types which are listed in order of increasing capacity: a standard vehicle (Canadian
33 Light Rail Vehicles - CLRV), an articulated vehicle (Articulated Light Rail Vehicles- ALRV),
34 and a new low-floor articulated vehicle (Flexity Outlook) that was just introduced in 2014. The
35 majority of streetcar routes operate on a shared right of way. However, there are a few that
36 operate on a dedicated right of way and some on a hybrid right of way with portions that are
37 dedicated and others shared.

38 The TTC publishes a daily customer service score card that shows how well it meets its
39 target goals (7). Its goal for the streetcar service is to provide on-time departures from end
40 terminals at least 90% of the time. However, the streetcar service performance continues to
41 hover around the 50-60% range, falling well short of its 90% goal. Therefore, in an effort to
42 improve service, the TTC plans to replace its old fleet with over 200 Flexity vehicles on a
43 gradual basis. The TTC believes that the higher capacity vehicle will reduce bunching on its
44 network (7). This is because the new vehicles will be operated with longer headways compared
45 to the ones currently in effect, while maintaining the same route capacity. The City of Toronto is
46 also currently in the process of constructing the Eglinton Crosstown, a new high-end light rail
47 line, and it is planning the addition of more light rail routes (Finch West LRT and Sheppard East

1 LRT). Therefore, with the expected growth of the network and the city population, it is more
2 critical now than ever to have a clear understanding of the factors that influence streetcar
3 bunching to ensure a better service operation overall. This will help transit agencies, including
4 the TTC, minimize the occurrence of bus bunching, which will likely lead to better service
5 efficiency and higher rider satisfaction.

6 This research aims at understanding the factors that impact the likelihood of streetcar
7 bunching within the City of Toronto. It also explores in more detail the external and internal
8 factors that impact the time to the initial bunching incident. The first model explores the odds of
9 a headway becoming a bunching incident, irrespective of the location of the incident. The
10 knowledge gained from this model could help transit operators formulate policies and strategies
11 to reduce the occurrence of bunching incidents. The second model estimates the time to the
12 initial bunching incident, given that one occurs. The later a bunching incident occurs, the better
13 it is for the operator; in other words, it is extremely useful to formulate policies that delay the
14 onset of bunching and its detrimental effects as far down the line as possible knowing that
15 bunching cannot be eliminated completely. The second model can help inform and guide such
16 strategies. The combined results of the two models can help inform policies that minimize the
17 occurrence of bunching and delay their onset if they do occur.

18 19 **LITERATURE REVIEW**

20 A sizable body of the transit literature has focused on bus bunching in terms of generating and
21 proposing several holding strategies to reduce bunching once it has occurred. For example,
22 Daganzo has developed several studies that provide theoretical holding techniques and other
23 corrective actions to deal with bus service bunching (8, 9). Daganzo and Pilachowski proposed a
24 control strategy whereby bus speeds are adjusted to maintain headways and consequently, reduce
25 bus bunching (10). Similarly, Moreira-Matias et al. and Liang et al. have developed different
26 theoretical methods to handle bunching once it has occurred (11, 12). Other researchers have
27 focused on exploring the factors that affect bus service travel, running time and dwell time (13,
28 14).

29 Despite these previous efforts, there is little that has been done on understanding the
30 causes and factors that impact bus bunching. There is also an absence of research on estimating
31 the time until a bunching incident occurs and the factors that impact this. In fact, only a few
32 studies can be found in the literature that investigated bus bunching using statistical analyses.
33 One of them is done by Mandelzys & Hellinga (15), where they attributed bus bunching to
34 fluctuating travel times between stops and dwell times. These characteristics were also attributed
35 to bus bunching in (16, 17). Diab et al. (1) developed a bus bunching model that was used to
36 investigate several factors such as passenger volume, delay at start, and their impact on the
37 probability of bunching. In contrast to work that has been done regarding bus bunching, it is rare
38 to find articles on streetcar bunching.

39 Other researchers have focused on understanding the impacts of several factors on
40 streetcar service performance, but not specifically on streetcar bunching. For example, Currie has
41 generated multiple articles regarding the impacts of different factors on streetcar service
42 performance. He explored streetcar safety (18), weather impacts (19), and dwell times (20, 21)
43 and compared streetcar performance in different countries (22, 23). He also discussed how transit
44 signal priority (TSP) handles bunched streetcar vehicles (24). Ling and Shalaby developed a
45 reinforcement learning approach to control streetcar bunching (25). With this very little research
46 on streetcar service operations, and even lesser on streetcar bunching, a better understanding of
47 the streetcar service bunching is needed. With the availability and the accuracy of AVL data, we

1 are now able to investigate streetcar bunching, while isolating the effects of different influential
 2 variables on the service.

3 Similar to streetcar bunching, the application of survival analysis in bunching incidents
 4 has not been explored before. Survival analysis was applied to the disruption duration in the
 5 TTC’s subway system (26) and provided a satisfactory model to predict the effects of different
 6 factors on disruption durations. In Yu et al.’s (27) work, bus travel time predictions and
 7 associated uncertainties were generated from survival analysis. Survival analysis seemed to
 8 provide promising results in both studies and has much potential for its application in our study
 9 to investigate the time it would take for two vehicles to bunch.

10

11 **METHODOLOGY**

12 The objectives of this analysis is to understand the general factors that impact the likelihood of
 13 streetcar bunching as well as to investigate in more detail the external and internal factors that
 14 impact the time to bunching. The data used in the analysis come from the TTC’s AVL system
 15 for eight streetcar routes within the City of Toronto for the last week of January 2016. The routes
 16 are 501, 504, 505, 506, 509, 510, 511 and 512; they are highlighted in Figure 1. The other three
 17 routes that were removed from the analysis (i.e., routes 502 and 503) were operated only by
 18 buses due to a shortage of streetcar vehicles at that time or was completely new (i.e., Route 514).
 19 The TTC’s AVL system records each vehicle’s location every 20 seconds. The acquired data
 20 included both weekends and weekdays, with a total of six million observations. The week
 21 chosen for data collection had mild and clear weather with minimal track construction, closures,
 22 or diversions. The eight routes included in the analysis are all high frequency routes, operated
 23 every 10 minutes or better anytime of the day every day of the week (28). Each streetcar route
 24 operates using one or a combination of the three different vehicle types mentioned in the
 25 introduction.

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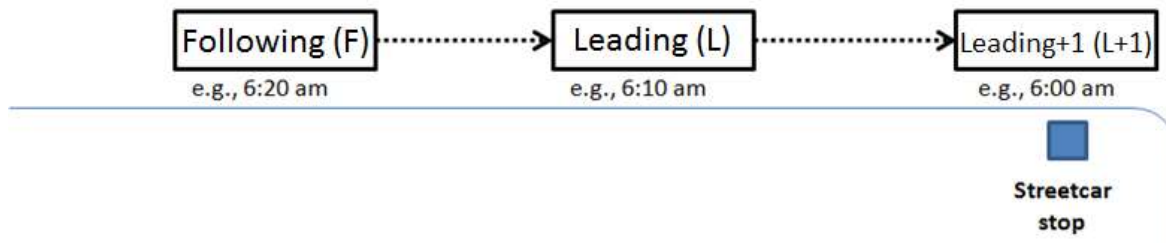
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30 **FIGURE 1 Map of TTC Streetcar Routes Included in the Study**

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32 The unit of analysis in this paper is the headway between consecutive vehicles. Since
 33 streetcars cannot overtake one another, the study focuses on the location when any pair of
 34 consecutive streetcars first form a bunch on the route. Bunching incidents were isolated at the
 35 segment level. A bunching incident is defined to be when the actual headway between two
 36 vehicles is less than half of the scheduled headway. To assist in understanding the dynamic
 37 factors that influence the streetcar bunching phenomenon, information about the previous

1 headway of a bunching occurrence is also used. The headway (or vehicles) is labelled as shown
 2 in Figure 2 to better understand the methodology. The vehicle in question is labelled as
 3 Following (F), vehicle in front of it is labelled Leading (L), and vehicle prior to the Leading is
 4 labelled as Leading+1 (L+1). If a bunching incident was observed between F and L, the headway
 5 between L and L+1 was considered as a predictor in the models. The underlying rationale is that
 6 if the Leading+1 vehicle is leaving the terminal early and the Leading vehicle is slightly late, the
 7 latter will likely pick up more passengers in addition to its normal load, leading to more delays
 8 for itself. Meanwhile, the Following vehicle (vehicle in question) will find fewer passengers to
 9 serve along the route even if it is leaving the terminal on time, increasing the odds of bunching
 10 with the Leading vehicle at a point down the line. Furthermore, the time to the initial bunching
 11 incident is defined to be the time it takes for the first bunching incident (as opposed to
 12 subsequent bunching incidents) in a trip to occur. The time is measured from the instant the
 13 Following streetcar leaves its route terminal to the instant it first catches up with the Leading
 14 streetcar.
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18 **FIGURE 2 Streetcar Vehicle Labelling System**

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20 The first model is a binary logistic regression model that investigates the effects of
 21 different factors on the likelihood of a streetcar bunching. Headways that experienced bunching
 22 and those that did not experience bunching were included in this model. Many variables were
 23 tested but were eliminated from the model due to insignificance such as schedule deviation for
 24 both the following and leading vehicle as well as headway ratios. Squared terms of some
 25 independent variables were used to account for a possible non-linear relationship between each
 26 variable and the dependent variable, if such a relationship existed. In addition to the route
 27 number, direction, day of the week and time of day variables, other variables were utilized in the
 28 models.

29 A set of headway deviation dummy variables were used in the model to reveal the impact
 30 of different combinations of headway deviations on bunching. Headway deviation is measured at
 31 the terminal and is categorized into three classes: shorter than scheduled headway, same as
 32 scheduled headway, or longer than scheduled headway. Headways that fall between 80-120% of
 33 the scheduled headway are defined to be the same as scheduled headway or on time. Headways
 34 that are less than 80% are defined to be shorter than scheduled headway and those greater than
 35 120% are longer than scheduled headway. These values were arbitrarily chosen, but seemed
 36 logical as some tolerance is required in defining on-time performance.

37 The second model, an AFT model, was used to explore the impact of both internal and
 38 external factors on the time to the first bunching incident for pairs of successive streetcars. The
 39 time is calculated from the terminal to the following vehicle it first bunched with the leading
 40 vehicle. Therefore, the model only focuses on the first location where bunching began to occur.
 41 In this model, only bunched trips were used. The AFT models are typically used in medicine to

1 analyze the time to an event, which is usually death or failure. In our case, a bunching incident
 2 can be considered as a failure event. External factors such as traffic volume, existence of transit
 3 signal priority, and the number of signalized intersections were included in this model. The
 4 internal factors discussed above were also included in the model. A detailed description of the
 5 variables used in both models can be found in Table 1.

6
 7 **TABLE 1 Description of the Independent Variables Used in the Models**
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Variable Name	Variable Type	Description
Weekday/Weekend	Dummy	Weekend (0) or weekday (1)
Trip Direction	Dummy	Eastbound/Southbound (0) or Westbound/Northbound (1)
Vehicle Combination	Categorical	Following & leading are same vehicle type = 0 Following vehicle capacity is larger than leading vehicle capacity = 1 Following vehicle capacity is smaller than leading vehicle capacity = 2
Time Period	Categorical	AM Peak=1, Midday=2, PM Peak=3, Evening = 4
Route #	Categorical	Streetcar route number; it captures route characteristics such as route length, right of way and average stop distance
Following & Lead Headway Ratio	Continuous	Ratio of actual F, L vehicle headway to the scheduled headway
Lead & Lead+1 Headway Ratio	Continuous	Ratio of actual L, L+1 vehicle headway to the scheduled headway
Scheduled Headway	Continuous	Scheduled headway between vehicles
Scheduled Headway ²	Continuous	Squared value of scheduled headway
Cumulative TSP	Continuous	Number of intersections equipped with transit signal priority between the terminal and bunching location
Stop Combination	Continuous	Stop placement at route level: if same stop (all near or all far side) placement (0), Combination of near and far side stops (1)
Cumulative Pedestrian Crossing	Continuous	Number of pedestrian crossings between the terminal and the bunching location
Cumulative Signalized Approaches	Continuous	Number of signalized intersections between the terminal and the bunching location
Traffic Volume	Categorical	Traffic volume is define to be a proportion of the highest volume. Low volume (0-33% of highest volume) (0), medium volume (34-66%) (1), high volume (67-100%) (2)

Lshort	Dummy	Leading vehicle is not short turned from the opposite direction (0), leading vehicle is short turned (1)
Short/Short	Dummy	Actual headway between F, L is shorter than scheduled headway and actual headway between L, L+1 is shorter than scheduled headway at terminal
Short/On Time	Dummy	Actual headway between F, L is shorter than scheduled headway and actual headway between L, L+1 is the same as scheduled headway at terminal
Short/Long	Dummy	Actual headway between F, L is shorter than scheduled headway and actual headway between L, L+1 is longer than scheduled headway
On Time/Short	Dummy	Actual headway between F, L is the same as scheduled headway and actual headway between L, L+1 is shorter than scheduled headway at terminal
On Time/ On Time	Dummy	Actual headway between F, L is the same as scheduled headway and actual headway between L, L+1 is the same as scheduled headway at terminal
On Time/Long	Dummy	Actual headway between F, L is the same as scheduled headway and actual headway between L, L+1 is longer than scheduled headway at terminal
Long/Short	Dummy	Actual headway between F, L is longer than scheduled headway and actual headway between L, L+1 is shorter than scheduled headway at terminal
Long/On Time	Dummy	Actual headway between F, L is longer than scheduled headway and actual headway between L, L+1 is the same as scheduled headway at terminal
Long/Long	Dummy	Actual headway between F, L is longer than scheduled headway and actual headway between L, L+1 is longer than scheduled headway at terminal
Route 501 x Short/Short	Dummy	An interaction variable between trips that belong to Route 501 and also experience shorter than scheduled headways

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2 **ANALYSIS**

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4 **Descriptive Statistics**

5 Table 2 shows the summary statistics of the trips used in the study and the % of bunched
6 headways per route. If a headway experiences bunching in any segment (i.e. less than half the
7 scheduled headway), it is considered a bunched headway. In total, about 30,500 headways were
8 included in the analysis. The majority of the analyzed headways occurred on weekdays. Out of
9 the total number of headways, approximately a quarter of them were involved in a bunching
10 incident. Route 504, with the highest ridership in Toronto (65,000 riders per day), experiences
11 the highest number of bunched headways (38.9%).

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TABLE 2 Descriptive Statistics of Headways Used in Models

Route	Direction		Day		Time Period				Grand Total	Bunching Events	% bunch
	EB/SB	WB/NB	Week end	Week day	AM Peak	Mid day	PM Peak	Evening			
501	3894	3880	1006	6768	1282	2242	1602	2648	7774	2141	27.5%
504	2918	2662	543	5037	1156	1367	1284	1773	5580	2171	38.9%
505	1313	1279	399	2193	423	791	505	873	2592	508	19.6%
506	1154	1080	260	1974	482	750	470	532	2234	839	37.6%
509	1212	1210	409	2013	331	732	610	749	2422	877	36.2%
510	1711	1715	554	2872	430	1213	779	1004	3426	741	21.6%
511	1242	1197	354	2085	432	724	483	800	2439	415	17.0%
512	2034	2004	468	3570	742	1183	864	1249	4038	65	1.6%
Total	15478	15027	3993	26512	5278	9002	6597	9628	30505	7757	25.4%
%	50.7%	49.3%	13.1%	86.9%	17.3%	29.5%	21.6%	31.6%	na	na	na

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Bunching Probability Model

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In this model, headways that have experienced bunching are coded as “1” and those that have not experienced bunching are coded as “0”. The results of this model are reported in Table 3. Variables that are found to be statistically significant of at least 90% are bolded in the table. This model has a Nagelkerke R Square value of 0.59, which indicates that 59% of the variance has been explained by the model. This R square value is comparable to other binary logistic models that investigate on-time performance (1, 29).

The route number variables, which have been included in the model as control variables, show a significant coefficient. This is expected since each route has different right of way characteristics, length, as well as the average stop distance. As shown in the descriptive statistics, Route 512 experienced the least amount of bunching, and therefore this model shows that all other routes have higher odds of bunching compared to this route. The model also indicates that the odds of bunching are higher on weekdays compared to the weekend. This is expected as there is an increase in ridership, frequency and traffic congestion during the week than the weekend. In addition, the midday, PM peak, and evening time periods were found to increase the odds of bunching compared to the AM peak. The increased chances of bunching frequency in the midday and evening peaks are likely due to the combined effect of the relatively high streetcar frequencies with lower volumes of the general traffic. .

Interestingly, the model shows that when the following vehicle has a greater capacity than the leading vehicle, this reduced the odds of bunching by 24%. This can be explained by the fact that since the following vehicle has a higher capacity, it will be able to hold more passengers and thus have a longer dwell time as well as total travel time. These longer times will prevent it from catching up with the leading vehicle. However, when the following vehicle has a lower capacity than the leading vehicle, the odds of bunching are increased by 124%. This is due to the fact that the leading vehicle will likely have longer dwell times, making it easier for the following vehicle to catch up and bunch with it. To summarize, both of the previous cases indicate that vehicles

1 with higher capacity are slower, and therefore they bunch with the following ones while
 2 increasing the headway gap with the leading ones.

3 The model indicates that for every minute that scheduled headway is increased, the odds
 4 of bunching is reduced by 44%, which is expected and was found in the bus literature (1).
 5 Therefore, schedule design plays a big role in bunching for streetcar service, and transit agencies
 6 should address this problem. This can be done by providing higher volume vehicles with longer
 7 headways, which is currently the TTC’s plan (7). The dummy variable Lshort was added to the
 8 model to understand the effects of short-turning on bunching incidents. On routes 504 and 510,
 9 up to 20% of the vehicles are short-turned. The strategy of short-turning is used in streetcar
 10 operations to address a serious effect of bunching occurrence, namely the long gaps in service
 11 downstream of bunched vehicles. It is assumed that the TTC short-turning procedure is only
 12 implemented when there is a long gap ahead of a streetcar bunch extending into the opposite
 13 direction. The model indicates here that when the leading vehicle is short-turned, it decreases
 14 the odds of bunching by 64%. This is logical since the following vehicle will still have to go to
 15 the terminal and run back in the opposite direction, which will create a gap between originally
 16 bunched trips.

17 With respect to headway deviation at terminals, only five of the nine combinatory dummy
 18 variables were found to be significant. A pattern can be noted with the significant combinatory
 19 headway deviation variables: when the following vehicle has an actual headway that is shorter
 20 than the scheduled headway, the odds of bunching is increased and when the following vehicle
 21 has an actual headway that is longer than the scheduled headway, the odds of bunching is
 22 reduced. The headway deviation combination that increases the odds of bunching the most is
 23 when the following vehicle has a shorter headway and the leading vehicle has a longer headway
 24 at the terminal, increasing the odds of bunching by 146%. This scenario essentially represents
 25 when the leading vehicle is delayed at start and the following vehicle leaves early at start. When
 26 the leading vehicle is delayed, it is likely to pick up more passengers, thus experiencing longer
 27 dwell times. When the following vehicle leaves the terminal early, it has very fewer passengers
 28 to pick up and therefore can easily catch up to the leading vehicle. In contrast, when the
 29 following vehicle has a longer headway and the leading vehicle has a shorter headway, this
 30 situation provides the greatest reduction in the odds of bunching out of all the cases where the
 31 following vehicle has a longer headway. An interaction variable between route 501 and
 32 short/short headway deviation combination is included in the model due to the fact that route 501
 33 experiences a lot of short/short headway deviations and skews the results of the short/short
 34 variable.

35
 36 **TABLE 3 Streetcar Bunching Probability Model Results**
 37

	Coefficient	Wald	Significance	Odds Ratio	95% Confidence Interval	
					Lower	Upper
Wkday	2.15	2450.65	0.00	8.62	7.92	9.39
Trip direction	0.32	72.73	0.00	1.37	1.28	1.47
Lshort	-1.02	253.45	0.00	0.36	0.32	0.41
Vehicle Combination	(Reference to same vehicle type for both following and leading vehicles)					
FVehCap > LVehCap	-0.27	18.60	0.00	0.76	0.67	0.86

FVehCap < LVehCap	0.33	32.36	0.00	1.39	1.24	1.56
Time Period	(Reference to AM Peak)					
Mid Day	0.78	183.44	0.00	2.19	1.95	2.45
PM Peak	0.18	10.17	0.00	1.20	1.07	1.34
Evening	0.94	145.62	0.00	2.56	2.19	2.98
Route Number	(Reference to Route 512)					
Route 501	8.16	2121.09	0.00	3494.14	2469.15	4944.62
Route 504	3.12	547.37	0.00	22.62	17.42	29.37
Route 505	3.88	696.07	0.00	48.58	36.40	64.82
Route 506	4.94	1190.14	0.00	139.23	105.19	184.31
Route 509	3.88	747.04	0.00	48.53	36.73	64.10
Route 510	2.03	212.45	0.00	7.61	5.79	9.99
Route 511	2.49	305.49	0.00	12.05	9.11	15.92
Scheduled Headway	-0.59	938.62	0.00	0.56	0.53	0.58
Headway Deviation Combination	(Reference to On Time/On Time)					
Short/Short	0.00	0.00	0.96	1.00	0.83	1.22
Short/On Time	0.18	2.68	0.10	1.20	0.97	1.48
Short/Long	0.38	14.26	0.00	1.46	1.20	1.77
On Time/Short	-0.04	0.11	0.74	0.96	0.78	1.20
On Time/Long	0.05	0.18	0.67	1.05	0.84	1.32
Long/Short	-0.68	40.58	0.00	0.51	0.41	0.63
Long/On Time	-0.51	16.88	0.00	0.60	0.47	0.77
Long/Long	-0.27	6.26	0.01	0.76	0.62	0.94
Route 501 x Short/Short	-24.59	0.00	0.96	0.00	0.00	na
Constant	-0.45	6.29	0.01	0.64	na	na

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Bunching Survival Model

A linear regression model as well as an ordinal logit model were developed to try to investigate the impact of the internal and external factors on the time to bunching. However, both of these models resulted in very low R squared and ρ squared values. Thus, a survival analysis was attempted next to model the time to the first bunch along the route. The model used the AFT specification rather than the Cox Proportional Hazard specification, because the study was interested in understanding the impact of the various factors on the survival time, not the hazard ratios.

Different distributions were tested to find the best fit. Comparing the Akaike Information Criterion (AIC) values for each distribution, the loglogistic distribution was found to have the best fit and was thus chosen for this model. The loglogistic distribution had the lowest AIC value at 14907 compared to the lognormal (15487), weibull (14975), and exponential (18461) distributions. The output of this model is reported in Table 4. Bolded variables indicate statistical significance of at least 90%. The reference variables are kept the same as in the first model to allow for comparison. A negative coefficient of a variable in this model indicates that as the magnitude of the associated variable increases the departing streetcar from the terminal

1 will catch up with the leading streetcar (i.e. creating a bunching incident) sooner than later
2 compared to the baseline scenario. In other words, a negative coefficient indicates an accelerated
3 time to bunch (failure) or a reduction in the survival time. The acceleration factor is determined
4 by exponentiating the coefficient, e^{β} (30).

5 Since the weekday variable has a negative coefficient, this means that on weekdays initial
6 bunching incidents, when they happen, take place sooner (relative to the departure time of the
7 following vehicle from the terminal) compared to weekends. The acceleration factor of $e^{-0.038} =$
8 0.96 indicates that the survival time or time to bunch on a weekday is 0.96 as large as on a
9 weekend. However, this was not found to be statistically significant. This indicates that while
10 the odds of bunching are higher during weekdays (according to the previous model), these
11 weekday bunches also take a shorter time to occur (according to this model).

12 Compared to the time periods to the AM peak, the results show that during the midday,
13 PM peak, and evening periods initial bunching incidents take longer to happen compared to the
14 AM peak. The PM peak indicates that the time to bunching is increased by a factor of 1.67
15 compared to the AM peak. Again, the route numbers are included in the model as control
16 variables. Regardless of the vehicle type combinations, when the vehicle capacities are different,
17 the model indicates that the time to initial bunch will be accelerated compared to when they are
18 the same vehicle type for both following and leading vehicles. This is expected because the
19 differences in capacities will impact the dwell times and thus, time to bunching. Therefore, while
20 the previous model indicates a difference in the impact of the size of vehicle on the probability of
21 bunching, this model shows that when bunching occurs, it occurs quicker when combinations of
22 different vehicle types are involved compared to the case of only one type of vehicles along the
23 route.

24 Other internal variables such as scheduled headway, headway ratio between actual and
25 scheduled headway for the following and leading vehicle, as well as the cumulative number of
26 TSP-equipped intersections all indicated they would cause a longer time for the initial bunching
27 incident to occur. For every additional minute of scheduled headway, the survival time is 1.11
28 times longer. Increasing the number of TSP-equipped intersections and headway ratio do not
29 increase the time to initial bunching as much as increasing the scheduled headway, but they still
30 do prolong the time to initial bunching. This is logical since increasing the headway ratio would
31 imply an increase in the actual headway which is likely to prolong the time for two consecutive
32 streetcars to meet in a bunching incident. However, the model shows that a combination of
33 different stop placements will accelerate the time to initial bunching compared to when stops are
34 placed all on the same side, whether it be far or near side. This could be because when stop
35 placements are alternated, they can still be between two consecutive intersections (i.e. farside
36 stop followed by a nearside stop) thus allowing the following vehicle to catch up more easily
37 with the leading one.

38 In terms of the external factors, the cumulative number of pedestrian crossing and
39 signalized approaches also accelerate the time to initial bunching. This is likely due to the effect
40 of signalized approaches on interrupting streetcar movements. On routes that do not have
41 dedicated right of way, streetcars must interact with vehicular traffic. High vehicular traffic
42 actually increases the survival time by a factor of 1.30. This may sound counterintuitive but
43 makes sense because the more traffic there is, the more vehicles there will likely be between the
44 successive streetcars. A microsimulation model of streetcar operation in Toronto found similar
45 results (31). This increased number of traffic vehicles between streetcars will increase the time it
46 takes for a bunching incident to occur.

1 **TABLE 4: AFT Model Results**
2

Variable	Coefficient (β)	Standard Error	z	P>z	95% C.I.for Coefficient	
					Lower	Upper
Wkday	-0.038	0.02	-1.55	0.12	-0.09	0.01
Trip direction	0.044	0.02	2.99	0.00	0.02	0.07
TimePeriod	(Reference to AM Peak)					
Midday	0.129	0.02	5.89	0.00	0.09	0.17
PM Peak	0.154	0.02	7.28	0.00	0.11	0.20
Evening	0.066	0.03	2.54	0.01	0.02	0.12
Route	(Reference to Route 512)					
501	-0.196	0.10	-1.97	0.05	-0.39	0.00
504	0.639	0.09	6.87	0.00	0.46	0.82
505	0.286	0.11	2.68	0.01	0.08	0.50
506	0.109	0.11	1.04	0.30	-0.10	0.32
509	-0.180	0.10	-1.84	0.07	-0.37	0.01
510	0.162	0.10	1.71	0.09	-0.02	0.35
511	-0.078	0.10	-0.77	0.44	-0.28	0.12
VehCombination	(Reference to same vehicle type for both)					
FVehCap > LVehCap	-0.079	0.02	-3.67	0.00	-0.12	-0.04
FVehCap < LVehCap	-0.084	0.02	-4.30	0.00	-0.12	-0.05
SchedHead	0.101	0.05	2.22	0.03	0.01	0.19
SchedHead²	-0.011	0.00	-3.16	0.00	-0.02	0.00
FLHeadRatio	0.002	0.00	18.04	0.00	0.002	0.002
LL1HeadRatio	0.000	0.00	-0.44	0.66	0.00	0.00
CumTSP	0.077	0.00	23.79	0.00	0.07	0.08
StopComb	-0.373	0.13	-2.84	0.01	-0.63	-0.12
CumPedCross	-0.030	0.00	-7.09	0.00	-0.04	-0.02
CumSigApp	-0.006	0.00	-10.97	0.00	-0.01	-0.01
Traffic Volume Cat	(Reference to low traffic volume category)					
Medium Volume	-0.012	0.02	-0.74	0.46	-0.04	0.02
High Volume	0.267	0.04	6.84	0.00	0.19	0.34
Constant	1.909	0.16	11.97	0.00	1.60	2.22

3
4 **CONCLUSION**

5 The overall results indicate that transit operators of streetcar systems should pay more attention
6 to headway deviations at terminals particularly on weekdays. To reduce the likelihood of
7 bunching occurrence, they should try to ensure that headways at terminal are not shorter than
8 scheduled headway. Ensuring this will also lengthen the time to a bunching incident, if one
9 occurs. During the planning process, stop locations should also be considered carefully, since

1 different stop placements cause initial bunching incidents to occur sooner than later. Heavy
2 traffic volume delays the onset of initial bunching, but this may also cause longer than
3 anticipated travel times, which will also be a nuisance to passengers. In conclusion, it would be
4 best if the TTC focused on the factors that could provide the most improvement (decreased odds
5 of bunching and longer time to bunch) for both parties (operator and passenger) such as
6 scheduled headway adherence and changes in fleet for consistency.

7 Since it is rare to find streetcar bunching models in the literature, this paper provides
8 valuable insights into streetcar bunching. Nevertheless, with additional data such as passenger
9 volume, which were not available for this paper, the models can be improved to provide more
10 information to streetcar operators. The results from this study can be combined to build a real-
11 time predictive model for bunching, which can allow transit operators to act proactively with
12 expected bunching incidents. Such a model would be able to warn operators of potential and
13 upcoming bunching incidents and the time it would take for the bunching incident to occur with
14 a given accuracy.

15 The results and future work from this study provide great potential for streetcar operators.
16 Armed with the knowledge gained from this study, operators can make informed decisions when
17 trying to improve streetcar services or when planning and building new streetcar routes. This
18 will allow operators to make evidence-based decisions instead of ad-hoc ones; and, therefore,
19 they would be able to develop actual procedures or decision making processes to prevent and
20 reduce bunching. Analogous to a screening procedure developed to give patients early treatment
21 in an attempt to extend their life, a real-time predictive bunching model could “detect and cure”
22 vehicles from bunching and extend its time away from the terminal to provide an efficient transit
23 service to the public.

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28

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